# RadLoco: A Rapid and Low Cost Indoor Location-Sensing System

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- Data Collection
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- ECS 5th and 6th floors

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Motivation Current Technologies Problem Definition

# **Location Aware Computing**

# Motivation

Location aware computing consists of the use of location information to improve the value of a wireless network for the users

#### **Examples**

- providing navigation through unfamiliar environments
- dynamic pre-allocation of resources



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Motivation Current Technologies Problem Definition

# **Current Technologies for Location-Sensing**

# Global Position System (GPS) and Cellular Networks

poor location performance indoors

#### Nireless Local Area Networks

- Many environments have ubiquitous wireless networks
- Wireless network access is being incorporated into smaller mobile devices



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Motivation Current Technologies Problem Definition

# **Problem Definition**

# Problem

 The relationship between location and radio signal strength is highly non-linear and not known a priori.

Survey data collection is time consuming.

# Solution

- Use non-parametric **estimation technique** to reduce noise and required number of survey points.
- Sensory network of Ultrasonic/Radio devices to aid in rapid survey data collection.



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Overview Data Collection Location Estimation Simple Graphical Example

#### Location Sensing System Overview



#### Details

2 stages: Data Collection and Data Processing



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Data Collection: Cricket Sensory Network



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Overview Data Collection Location Estimation Simple Graphical Example

# **Cricket Sensory Network for Ground Truth Location**



# Sensory Network

- provide ground truth location for survey point.
- use modified steepest descent and Newton's method optimization

#### Cricket Details

- accuracy = mean accuracy of 14 cm
- sensors = ultrasonic (40 kHz), radio (433 MHz)
- **developers** = Networks and Mobile Systems Group at MIT.
- **cost** = \$3000 for 12 crickets covering 500  $m^2$

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Overview Data Collection Location Estimation Simple Graphical Example

#### Location Sensing System Overview



#### **Details**

Data Collection: WLAN



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Overview Data Collection Location Estimation Simple Graphical Example

# WLAN information

#### WLAN data

- RSS from base station
- MAC of base station
- Time
- SSID (network ID)

#### Survey Data

- WLAN data and ground truth location compose of a survey point.
- Collect several survey points within a floor or room to create a survey data set.



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#### Details

Data Processing: Location Estimation



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Overview Data Collection Location Estimation Simple Graphical Example

### **Location Estimation**

# **Estimation Algorithm**

Non-Parametric Kernel/Parzen Estimation Technique using a sum of multivariate Gaussian Distributions.

#### Variables

- **b** = vector of base stations (WLAN)
- *z* = vector of receive signal strength measurements (WLAN)
- $\theta = x \& y$  coordinates (survey points)
- $\hat{\theta} = x \& y$  coordinate (estimated location)



Overview Data Collection Location Estimation Simple Graphical Example

### **Location Estimation**



Overview Data Collection Location Estimation Simple Graphical Example

# Simple Graphical Example



#### **Explanation**

#### 3 base stations and 4 cricket sensors

Overview Data Collection Location Estimation Simple Graphical Example

#### Simple Graphical Example



#### **Explanation**

crickets provide ground truth location (blue dots)



Overview Data Collection Location Estimation Simple Graphical Example

#### Simple Graphical Example



#### Explanation

base stations provide RSS vector (z)



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Overview Data Collection Location Estimation Simple Graphical Example

# Simple Graphical Example



#### **Explanation**

take RSS measurement at current unknown location



Overview Data Collection Location Estimation Simple Graphical Example

# Simple Graphical Example



#### **Explanation**

and use the survey points collected prior



Overview Data Collection Location Estimation Simple Graphical Example

#### Simple Graphical Example



#### **Explanation**

to calculate the weight from z feature and Kernel estimator



Overview Data Collection Location Estimation Simple Graphical Example

#### Simple Graphical Example



#### **Explanation**

estimated location is calculated using weights and  $\theta$  feature



ECS Room 116 ECS 5th and 6th floors

# ECS 116 - Experimental Setup

#### Environment

- Engineering and Computer Science building lecture hall 116
- 117 seats divided into 8 rows
- 10 x 13 meters with 2 seats/m

#### Equipment

- hardware: Dell Inspiron laptop + Intel 802.11g WLAN card
- software: Netstumber, Radloco, MySQL



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# **ECS 116 - Experimental Results**



# Description

- We were able to obtain over 80% accuracy within 4 meters or 6 seats.
- Motivation for ECS 5th and 6th floor



ECS 5th and 6th floors

Conclusions

ECS 5th and 6th floors - Experimental Setup

# Environment

- Building has an atrium like structure
- Experiments were restricted to hallways and public conference rooms.

- WAPs from networks UVicOpen or engrnet.
- more than 35 unique WAPs and minimum of 12 WAPs



ECS 5th and 6th floors

Conclusions

ECS 5th and 6th floors - Experimental Setup

# Environment

- Building has an atrium like structure
- Experiments were restricted to hallways and public conference rooms.

# **Base Station (WAP) Information**

- WAPs from networks UVicOpen or engrnet.
- more than 35 unique WAPs and minimum of 12 WAPs visible at any location on a floor.



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ECS Room 116 ECS 5th and 6th floors

Conclusions

#### **Experimental Results - Decimation of Survey Set**



#### Description

Decimating survey set yields near identical performance.



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ECS Room 116 ECS 5th and 6th floors

#### Experimental Results - 6th vs. 5th floor



#### Description

# Both floor have similar accuracy of **3.5 m** more than 80% of the time.



ECS Room 116 ECS 5th and 6th floors

Conclusions

#### **Experimental Results - Number of Base Stations**



#### Description

Increasing base stations yields better accuracy



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ECS Room 116 ECS 5th and 6th floors

Conclusions

#### **Experimental Results - Combined Datasets**



### Description

Combined floors data sets provides 3D location accuracy with over **98% floor accuracy** 



# Conclusions

#### **Major Contributions**

- location-sensing system that locates mobile computing devices indoors based on WLAN technology.
- sensory network composed of radio/ultrasonic devices allow rapid data collection
- 98% accuracy floor accuracy and location estimations within 3.5m of true location



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### Conclusions

#### **Further Research**

- IEEE 802.16, WIMAX, can be extended for indoor location.
- sensory network calibration on walls

real-time location estimation for the RadLoco software



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# Conclusions

#### **List of Publications**

- Eugene Hyun, Michael McGuire, Mihai Sima, "RadLoco: A Rapid and Low Cost Indoor Location-Sensing System" IEEE 3rd International Conference on Communications and Networking in China, Hangzhou, Aug 2008.
- Michael McGuire, Eugene Hyun, Mihai Sima, "Location Aware Computing for Academic Environments" The 3rd International Conference on Quality of Service in Heterogeneous Wired/Wireless Networks (MobConQoE '07), Vancouver, Canada, Aug 2007.
- Eugene Hyun, Diego Felix, Michael McGuire, Mihai Sima, "A Three-Dimensional Indoor Location-Sensing using Radio and Ultrasonic Sensing Technologies", ETRI Journal (in Preparation)
- Eugene Hyun, Mihai Sima, Michael McGuire, "Reconfigurable Implementation of Wavelet Transform on an FPGA-Augmented NIOS Processor", IEEE Canadian Conference on Electrical and Computer Engineering (CCECE '06), Ottawa, Canada. May 2006, pp. 1052-1055.



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#### Thank you!



# Thank you!



# **Block Diagram of Estimated Location**



### weighted average function

$$w_i = \frac{\mathsf{K}(\boldsymbol{x} - \boldsymbol{X}_i)}{\sum_{i=1}^{N} \mathsf{K}(\boldsymbol{x} - \boldsymbol{X}_i)}$$

(1)

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#### **Software Setup**



#### steps

#### start Netstumbler and load Radloco perlscript

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#### **Software Setup**



#### steps

#### load map into Radloco and click on map to record data



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#### **Software Setup**



#### steps

#### crickets provide ground truth coordinates

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#### **Software Setup**



#### steps

RSS, BSSID and coordinates are saved to MySQL database



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#### **Software Setup**



#### steps

#### data processing is performed in Matlab



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**Bayesian Estimation Algorithm - 1** 

#### Minimum Mean Square Estimate (MMSE)

The MMSE of the terminal location is

$$\hat{\theta}_{MMSE} = E[\theta|\boldsymbol{x}] = \int_{S} \theta f_{\Theta}(\theta|\boldsymbol{x}) d\theta$$
 (2)

The above equation can be expanded to

$$\hat{\theta}_{\text{MMSE}} = \int_{S} \theta \frac{f_{\boldsymbol{X},\Theta}(\boldsymbol{x},\theta)}{f_{\boldsymbol{X}}(\boldsymbol{x})} d\theta = \frac{\int_{S} \theta f_{\boldsymbol{X},\Theta}(\boldsymbol{x},\theta) d\theta}{f_{\boldsymbol{X}}(\boldsymbol{x})} = \frac{\int_{S} \theta f_{\boldsymbol{X},\Theta}(\boldsymbol{x},\theta) d\theta}{\int_{S} f_{\boldsymbol{X},\Theta}(\boldsymbol{x},\theta) d\theta}$$
(3)

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**Bayesian Estimation Algorithm - 2** 

Minimum Mean Square Estimate (MMSE)

The joint approximate PDF is given by

$$\hat{f}_{\Theta,\boldsymbol{X}}(\boldsymbol{\theta},\boldsymbol{X}) = \frac{1}{N}(h_{X})^{-L}(h_{\theta})^{-2}\sum_{i=1}^{N}\mathsf{K}_{\boldsymbol{X}}\left(\frac{\boldsymbol{X}-\boldsymbol{X}_{i}}{h_{X}}\right)\mathsf{K}_{\Theta}\left(\frac{\boldsymbol{\theta}-\boldsymbol{\theta}_{i}}{h_{\theta}}\right)$$
(4)

with  $K(\cdot)$  being the Kernel functions for location and RSS measurements. The value *L* represents length of vector **x**.

#### **Kernel Function**

For the kernel functions  $K(\cdot)$  we use the standard multivariate Gaussian distribution:

$$K_{\boldsymbol{X}}(\boldsymbol{x}) = \left(\frac{1}{\sqrt{2\pi}}\right)^{L} \exp\left(-\frac{1}{2}(\boldsymbol{x}^{T}\boldsymbol{x})\right)$$

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(5)

# **Bayesian Estimation Algorithm - 3**

#### Joint approximate PDF

If we substitute the estimated PDF from Equation (4) into (3) and perform integration by substitution using  $\boldsymbol{u} = \boldsymbol{\theta} - \boldsymbol{\theta}_i$ , we can reduce:

$$\int \boldsymbol{\theta} \,\mathsf{K}_{\Theta} \left(\boldsymbol{\theta} - \boldsymbol{\theta}_{i}\right) d\boldsymbol{\theta} = \int \left(\boldsymbol{u} + \boldsymbol{\theta}_{i}\right) \mathsf{K}_{\boldsymbol{U}}(\boldsymbol{u}) d\boldsymbol{u} = \boldsymbol{\theta}_{i} \tag{6}$$

since the mean of the random variable **U** is:

 $\int \boldsymbol{u} K_{\boldsymbol{v}}(\boldsymbol{u}) d\boldsymbol{u} = 0$ 

and

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# **Bayesian Estimation Algorithm - 4**

#### Minimum Mean Square Estimate (MMSE)

The resulting estimated location  $\hat{\theta}$  is then a weighted average where the sum is taken across the weighted locations in the subset:

$$\hat{\theta} = \sum_{i=1}^{N} w_i \theta_i \tag{7}$$

(8)

with the weights  $w_i$  for each survey point *i* being defined as:

$$w_i = \frac{\mathsf{K}(\boldsymbol{x} - \boldsymbol{X}_i)}{\sum_{i=1}^{N} \mathsf{K}(\boldsymbol{x} - \boldsymbol{X}_i)}$$

#### **Kernel Width**



# Kernel width

Small values of  $h_x$  indicate that the RSS vectors can change radically with short spatial displacements of the mobile device while larger values indicate that the RSS changes significantly only with large spatial displacements.



### **Kernel Width**

#### **Optimal Kernel Width**

- two datasets are needed for training:
  - survey set dataset A
  - 2 validation set dataset B.
- Each location in dataset B estimated using Kernel Estimator with survey dataset A, while varying the parameter h<sub>x</sub>.
- The h<sub>x</sub> that produces the minimum MSE is the optimal kernel width for the training dataset B.
- In theory, we need a training set of infinite size to determine optimal kernel. Therefore optimal means best kernel given our finite datasets.
- A third dataset C can be used for verification and is considered the test dataset. The set C is not used for training because it would extend the survey set.



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### **Kernel Width**

#### **Cross-Validation**

 collecting multiple datasets may be costly and time consuming: determine the optimal kernel width h<sub>x</sub> for one dataset using a cross-validation approach.

$$MSE(h) = \sum_{i=1}^{N} \left[ \theta_i - \sum_{k=1,\neq i}^{N} w_k \theta_k \right]^T \times \left[ \theta_i - \sum_{k=1,\neq i}^{N} w_k \theta_k \right]$$
(9)

 remove a survey point from the survey set, then estimating the location of the survey point using the rest of the survey points, while varying h<sub>x</sub> values.



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#### **Error Calculation**



green dot = true location red dot = estimated location

#### **Error Calculation**



# **Error Calculation**

