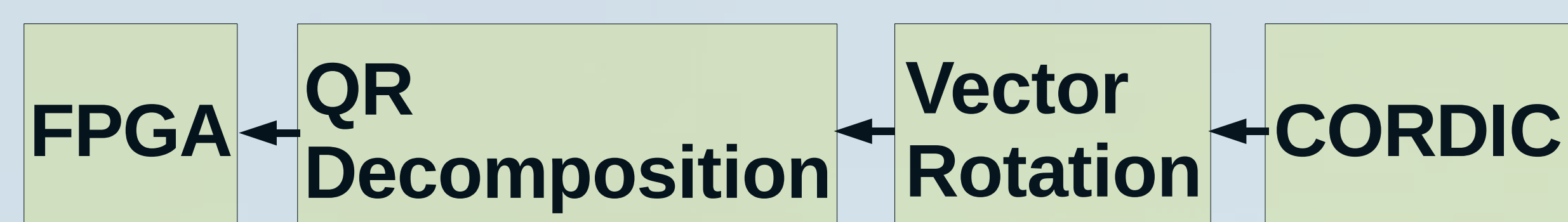


Introduction

- Following the project theme of **Intelligent Systems and Sensors**, used to increase the **safety** of modern vehicles
- Overall project: **Inertial Sensor Cluster for Adaptive Path Prediction**
- Dynamic model is a set of differential equations describing the maneuvering capabilities of the vehicle
 - **Kalman filter**. Computationally intensive: Use FPGA



- Many common mathematical operations are required in the course of computing a complex algorithm. To maximize overall efficiency, these operations themselves must be as efficient as possible: consider CORDIC

CORDIC (COordinate Rotation DIgital Computer)

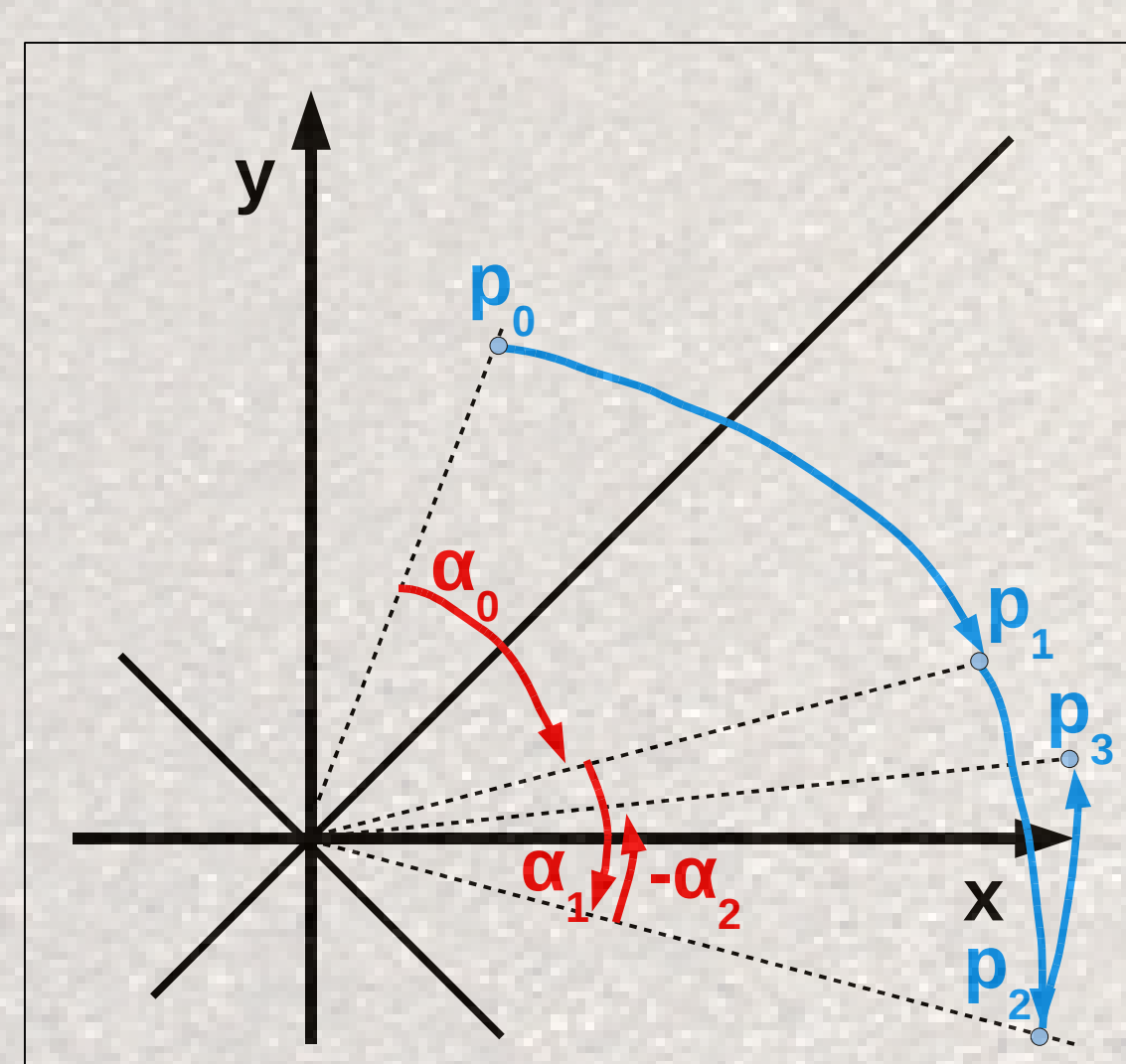
- CORDIC is a cheap method to compute many transcendental functions
 - Trigonometric and hyperbolic functions, as well as exponential functions, logarithms, multiplications, divisions, and square roots.
- **Advantages**
 - Requires no hardware multiplier; only shift, addition and subtraction operations, and table lookup are used
 - Therefore performs faster in most cases, (especially when no hardware multiplier is available)
 - Minimizes number of gates required to implement supported functions, most useful for FPGA applications
- **Disadvantages**
 - When hardware multiplier available can be slower than table lookup methods (eg in DSP microprocessor)

Method of Computation

- Using only bitshift and addition operations, (and LUT access) vectors can be rotated, due to rotation operation of:
 - $x^{(i+1)} = x^{(i)} - y^{(i)}\tan\alpha^{(i)}$;
 - $y^{(i+1)} = y^{(i)} + x^{(i)}\tan\alpha^{(i)}$;
 - $z^{(i+1)} = z^{(i)} - \alpha^{(i)}$;
 - Where $\tan\alpha^{(i)} = d_i \cdot 2^{-i}$, $d_i \in \{-1,1\}$

Example

- To compute the square root or magnitude of two numbers, a vector can be rotated to a point where $y = 0$, and $x =$ magnitude of vector, as in the adjacent figure
- Conversion between cartesian and polar co-ordinates is possible.

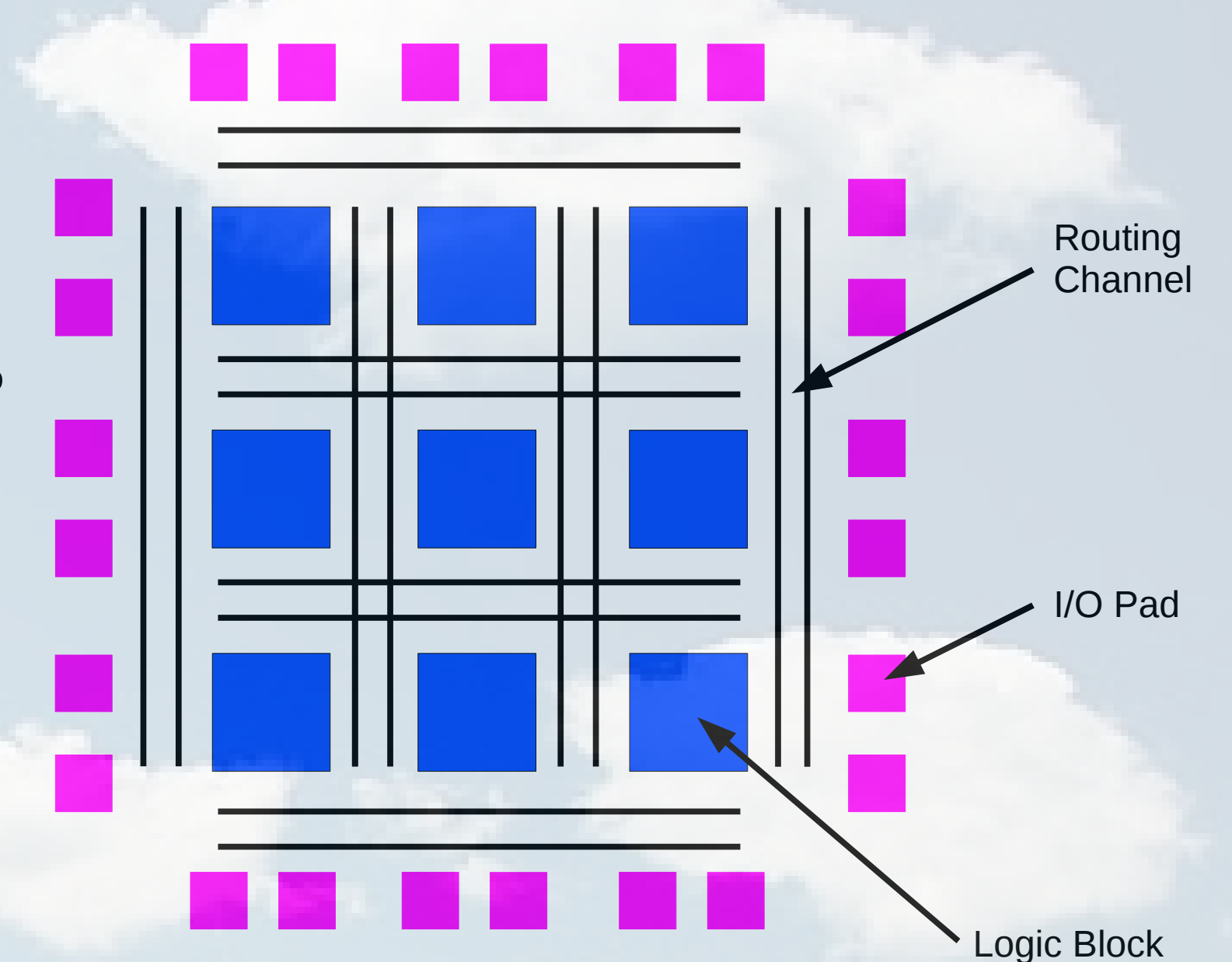


Precision

- CORDIC can compute to arbitrary precision, however, finite registers on processor limit precision of result
- Computation wise, at minimum, each additional bit of precision requires another iteration of processing

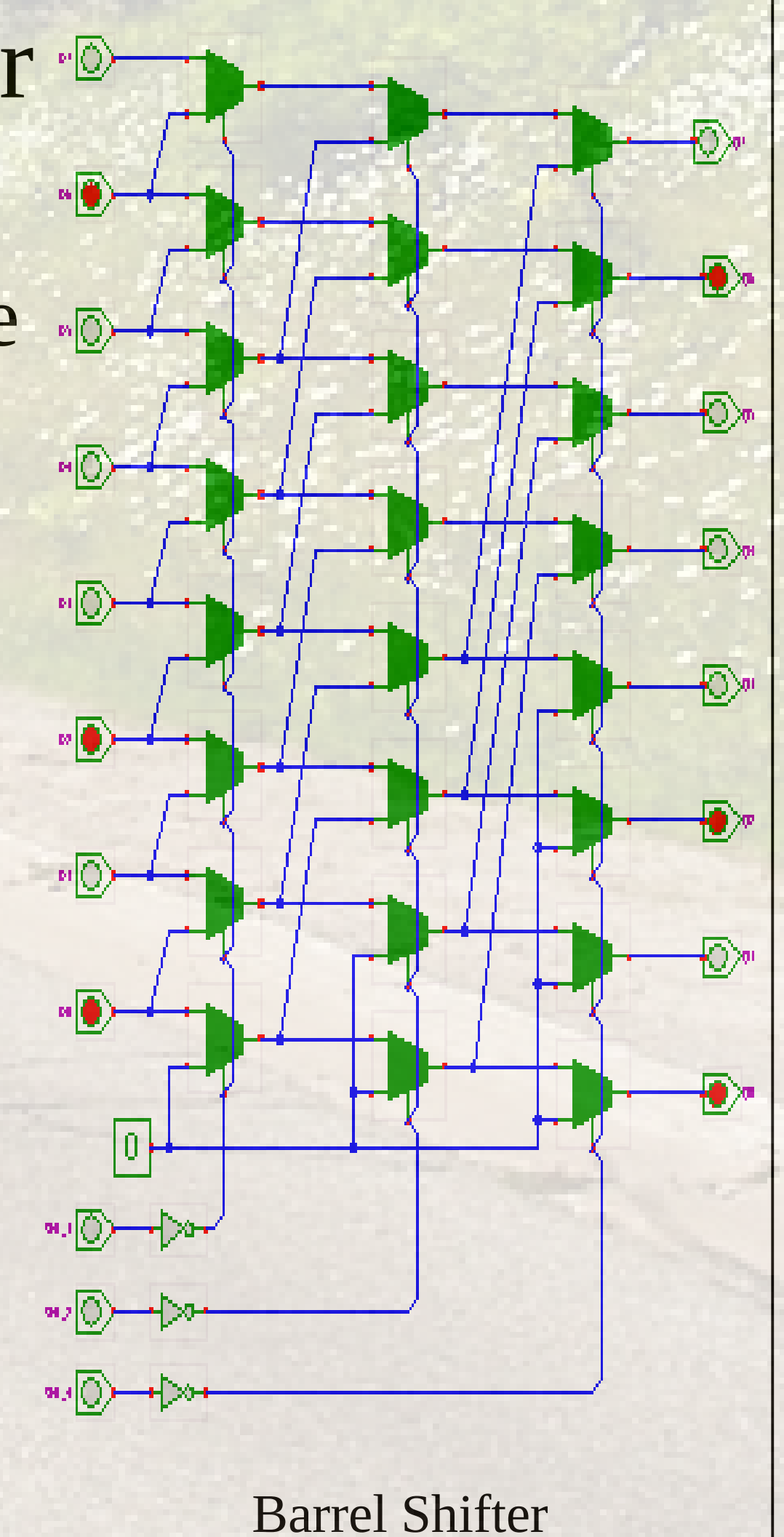
FPGA

- Field-programmable gate array is an integrated circuit that is configured after manufacturing, in “field”
- Contain programmable logic units which are “wired together” as in the following diagram
- Logic blocks can be configured to compute complex combinational functions or simple gates
- **Interconnects**
 - Are reconfigurable
 - Are slow
 - Main FPGA bottle-neck
 - Programmer must design to minimize interconnect usage



CORDIC on a FPGA

- Consists of **Barrel Shifter, adder, subtractor, and LUTs**
- **Barrel Shifter**
 - Three Options: Rolled, Unrolled and Partially Rolled
 - **Rolled**, Requires Barrel Shifter
 - Separate modules exist on FPGA
 - Less space but more interconnect use
 - Slower operation; signal travels between modules: interconnect use
 - Faster clock frequency
 - Not necessarily faster overall operation
 - **Unrolled**, No Barrel Shifter
 - Combinational method
 - Larger footprint
 - Slower clock frequency
 - Possibly faster overall computation
 - **Partially Rolled**
 - Combination of above two methods with more combinational parts than Rolled



Applications

- Trigonometric and hyperbolic functions as well as exponential functions, logarithms, multiplications, divisions, and square roots.
- Linear algebra, (QR, SVD)
- **Kalman filter for Adaptive Path Prediction**